

**ERRATUM TO “SOME REMARKS ON THE UNROLLED QUANTUM
GROUP OF $\mathfrak{sl}(2)$ ”**

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The following corrections should be made to the formulas in the published version of “Some remarks on the unrolled quantum group of $\mathfrak{sl}(2)$.” We apologize to the readers for the inconvenience.

- Formula (30) in page 3249 should be replaced by :

$$\Phi_{S_i, P_j} = (-1)^i \frac{\{(i+1)(j+1)\}}{\{j+1\}} \text{Id}_{P_j} + (-1)^i \{1\}^2 \frac{i\{(i+2)(j+1)\} - (i+2)\{i(j+1)\}}{\{j+1\}^3} x_j,$$

- Formula (31) in page 3249 should be replaced by :

$$\Phi_{V_0, P_j} = (-1)^{r+j} \frac{2r\{1\}^2}{\{j+1\}^2} x_j, \quad \Phi_{P_i, P_j} = \frac{(-1)^i 2r\{1\}^2}{\{j+1\}^2} \left(q^{(i+1)(j+1)} + q^{-(i+1)(j+1)} \right) x_j.$$

- Page 3250 line -15, replace the formula by :

$$\Phi_{S_i, P_j} = \frac{(-1)^i}{\{j+1\}} \left(\{(i+1)(j+1)\} \text{Id}_{P_j} + \frac{\{1\}^2 x_j}{\{j+1\}^2} (i\{(i+2)(j+1)\} - (i+2)\{i(j+1)\}) \right).$$

- Page 3250, line -13, replace the formula by :

$$\Phi_{V_0, P_j} = (-1)^{r+j} \frac{2r\{1\}^2}{\{j+1\}^2} x_j.$$

- Page 3250, line -9, replace the computation by :

$$\begin{aligned} \Phi_{P_i, P_j} &= \Phi_{V_0, P_j} (\Phi_{S_{r-i-1}, P_j} - \Phi_{S_{r-i-3}, P_j}) \\ &= \frac{-(-1)^{i+j} 2r\{1\}^2}{\{j+1\}^3} (\{(r-i)(j+1)\} - \{(r-i-2)(j+1)\}) x_j \\ &= \frac{-(-1)^{i+j} 2r\{1\}^2}{\{j+1\}^2} \left(q^{(r-i-1)(j+1)} + q^{-(r-i-1)(j+1)} \right) x_j \\ &= \frac{(-1)^i 2r\{1\}^2}{\{j+1\}^2} \left(q^{(i+1)(j+1)} + q^{-(i+1)(j+1)} \right) x_j. \end{aligned}$$

- Page 3250 line -5 replace the formula by :

$$\mathbf{t}_P(\Phi_{V_0, P}) = \mathbf{t}_{V_0}(\Phi_{P, V_0}) = (-1)^{r-1} \langle \Phi_{P, V_0} \rangle$$

- Page 3250 line -3 replace the computation by

$$\begin{aligned} \mathbf{t}_P(\Phi_{V_0, P}) &= \mathbf{t}_P(\text{ptr}_R(c_{P, V_0} c_{V_0, P})) = \mathbf{t}_{P \otimes V_0}(c_{V_0, P} c_{P, V_0}) = \mathbf{t}_{V_0 \otimes P}(c_{P, V_0} c_{V_0, P}) \\ &= \mathbf{t}_{V_0}(\text{ptr}_R(c_{P, V_0} c_{V_0, P})) = \mathbf{t}_{V_0}(\Phi_{P, V_0}) = (-1)^{r-1} \langle \Phi_{P, V_0} \rangle \end{aligned}$$

- Page 3251 line 5, replace $\mathbf{d}(V_0) = (-1)^{r-1} r$ by $\mathbf{d}(V_0) = (-1)^{r-1}$

- Page 3251 line 9, replace the formula with

$$d(P_j) = \mathfrak{t}_{P_j}(\text{Id}_{P_j}) = (-1)^{j+1}(q^{j+1} + q^{-j-1}) \quad \text{and} \quad \mathfrak{t}_{P_j}(x_j) = (-1)^{j+1} \frac{\{j+1\}^2}{\{1\}^2}.$$

- Page 3251 line 18, replace formula with :

$$(-1)^{r+j} 2r \mathfrak{t}_{P_j}(x_j) \frac{\{1\}^2}{\{j+1\}^2} = (-1)^{r-1} r \frac{2}{d(V_0)} \mathfrak{t}_{V_0}(\text{Id}_{V_0})$$

- Page 3251 line 21 replace the formula with :

$$\theta_{P_j} = (-1)^j q^{\frac{j^2+2j}{2}} (1 - (r-j-1)) \frac{\{1\}^2}{\{j+1\}} x_j.$$

- Page 3251 line -4, replace formula with:

$$\mathfrak{t}(\theta_{P_j}) = -q^{\frac{j^2+2j}{2}} (q^{j+1} + q^{-j-1} + \lambda \frac{\{j+1\}^2}{\{1\}^2})$$

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